

## **2. Operations Research Analysis**

Operations Research and the Management Sciences include a variety of problem-solving techniques focused on improved efficiency of systems and support in the decision-making process. The realm of Operations Research involves the construction of mathematical models that aim to describe and/or improve real or theoretical systems and solution methodologies to gain real-time efficiency.

The knowledge area of Operations Research is by its nature mathematical and computational. A fundamental basis in this knowledge area includes probability, statistics, calculus, algebra, and computing.

### **2.1. Operations Research**

- 2.1.1. Modeling approaches
- 2.1.2. Heuristic versus optimization procedures

### **2.2. Linear Programming (LP)**

- 2.2.1. LP applications
  - 2.2.1.1. Diet problem
  - 2.2.1.2. Work scheduling
  - 2.2.1.3. Capital budgeting
  - 2.2.1.4. Blending problems
- 2.2.2. LP modeling techniques
- 2.2.3. LP assumptions
- 2.2.4. Simplex method
- 2.2.5. Degenerate and unbounded solutions
- 2.2.6. Post-optimality and sensitivity analysis
- 2.2.7. Interior-point approaches
- 2.2.8. Duality theory
- 2.2.9. Revised simplex method
- 2.2.10. Dual simplex method
- 2.2.11. Parametric programming
- 2.2.12. Goal programming

### **2.3. Transportation Problem**

- 2.3.1. Transportation model and its variants
- 2.3.2. Transportation simplex method
- 2.3.3. Transshipment problems

### **2.4. Linear Assignment Problem**

- 2.4.1. Assignment model
- 2.4.2. The Hungarian algorithm

### **2.5. Network Flows and Optimization**

- 2.5.1. Shortest path problem

- 2.5.2. Minimum spanning tree problem
- 2.5.3. Maximum flow problem
- 2.5.4. Minimum cost flow problem
- 2.5.5. CPM and PERT problems
- 2.5.6. Network simplex method

## **2.6. Deterministic Dynamic Programming**

### 2.6.1. Applications

- 2.6.1.1. Knapsack/fly-away/cargo-loading problems
- 2.6.1.2. Workforce size problems
- 2.6.1.3. Equipment replacement problems
- 2.6.1.4. Investment problems
- 2.6.1.5. Inventory (see Operations Engineering & Management knowledge area)

### 2.6.2. Forward and backward recursions

## **2.7. Integer Programming**

### 2.7.1. Applications and modeling techniques

- 2.7.1.1. Capital budgeting
- 2.7.1.2. Set-covering and set-partitioning problems
- 2.7.1.3. Fixed-charge problem
- 2.7.1.4. Either-or and if-then constraints

### 2.7.2. Branch-and-bound algorithm

### 2.7.3. Cutting plane algorithm

### 2.7.4. Traveling salesman problem and solution methods

## **2.8. Nonlinear Programming**

### 2.8.1. Unconstrained algorithms

- 2.8.1.1. Direct search methods
- 2.8.1.2. Gradient methods

### 2.8.2. Constrained algorithms

- 2.8.2.1. Separable programming
- 2.8.2.2. Quadratic programming
- 2.8.2.3. Chance-constrained programming
- 2.8.2.4. Linear combinations method

## **2.9. Metaheuristics**

### 2.9.1. Steepest ascent and descent (Greedy algorithms)

### 2.9.2. Tabu search

### 2.9.3. Simulated annealing

### 2.9.4. Genetic algorithms

### 2.9.5. Ant colony optimization

### 2.9.6. Particle swarm techniques

## **2.10. Decision Analysis and Game Theory**

### 2.10.1. Multi-criteria decision making

- 2.10.2. Decision making under certainty
  - 2.10.2.1. Analytic hierarchy process
  - 2.10.2.2. ELECTRE
- 2.10.3. Decision making under risk and uncertainty
  - 2.10.3.1. Decision tree-based expected value criterion
  - 2.10.3.2. Utility theory
- 2.10.4. Two-person zero-sum and constant-sum games
- 2.10.5. Robust decision making

## **2.11. Modeling Under Uncertainty**

- 2.11.1. Stochastic processes
- 2.11.2. Markov chains
- 2.11.3. Chapman-Kolmogorov equations
- 2.11.4. States and properties
- 2.11.5. Stochastic programming

## **2.12. Queuing Systems**

- 2.12.1. Components of a queuing model
- 2.12.2. Relationship between the exponential and Poisson distributions
- 2.12.3. Birth-and-death process-based queuing models
- 2.12.4. Queuing models involving non-exponential distributions
- 2.12.5. Priority-discipline queuing models
- 2.12.6. Queuing networks

## **2.13. Simulation**

- 2.13.1. Monte Carlo simulation
- 2.13.2. Continuous and discrete time models
- 2.13.3. Simulation methodology
  - 2.13.3.1. Sampling from probability distributions
- 2.13.4. Random number generation

## **2.14. Fundamentals of Systems Dynamics**

- 2.14.1. Principles of systems dynamics
- 2.14.2. Balancing loops
- 2.14.3. Feedback loops

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